

Composite Materials: Analysis and Design

Homework no.6

Due Date: _____

Problem 1

A symmetric laminate is composed of four plies with ply angles $\pm \theta$. If the total thickness of the laminate is (t) , determine the individual thicknesses which guarantee that the laminate is orthotropic with respect to bending force. That is $D_{13}=D_{23}=0$.

Problem 2

Show that as the number of plies increases in a regular symmetric cross-ply laminate of given total thickness, $D_{11} \rightarrow D_{22}$.

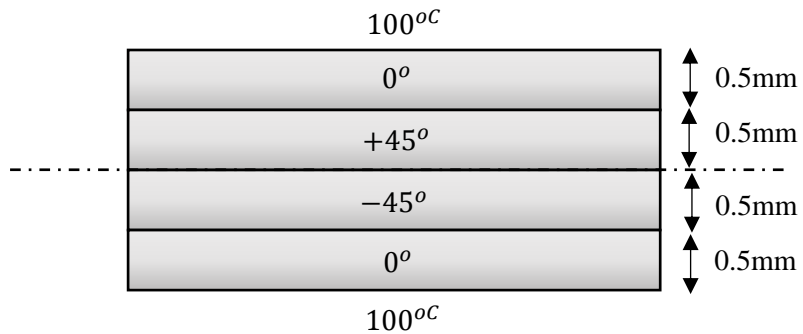
Problem 3

A thin flat sheet made from unidirectional fibers in a polymer matrix has the following elastic constants: $E_1 = 14^{GPa}$, $E_2 = 3.5^{GPa}$, $\nu_{12} = 0.4$, $G_{12} = 4.2^{GPa}$

In-plane loads are applied on x,y directions which make an angle of 60° to the principal directions. A compressive stress of 3.5MPa is applied on x direction, a tensile stress of 7MPa on y direction and a shear stress of 1.4MPa. Calculate the stresses and the strains in the principal directions, and also the strains on x,y directions.

Problem 4

The composite laminate is cured at 130°C and is being used in such conditions that are illustrated in the figure:



a. Calculate the strains and curvatures

b. Calculate and illustrate graphically the through-the-thickness local stress distribution.

$$E_{11} = 164.0 \text{ GPa}, E_{22} = 8.30 \text{ GPa}, G_{12} = 2.10 \text{ GPa}, \nu_{12} = 0.30$$

Thermal properties:

$$\alpha_1 = -4.5\text{e-}6 /^{\circ}\text{C}, \alpha_2 = 3.17\text{e-}5 /^{\circ}\text{C}$$